

1. Let  $A$  be the area bound by  $f(x) = 1 - x^2$ , the  $x$ -axis, and the  $y$ -axis. Find the volume of the solid of revolution formed by rotating  $A$  about the  $y$ -axis.
  - (a) Draw  $A$  and the solid of revolution. What shape are the cross sections?
  - (b) Find the area of an arbitrary cross-section  $A(y)$ .
  - (c) Calculate the volume of the solid by integrating  $A(y)$  over an appropriate interval.
  
2. Let  $A$  be the area bound by  $f(x) = \frac{x^2}{3}$  and  $g(x) = x$ . Find the volume of the solid of revolution formed by rotating  $A$  about the  $x$ -axis.
  - (a) Draw  $A$  and the solid of revolution. What shape are the cross sections?
  - (b) Find the area of an arbitrary cross-section  $A(x)$ .
  - (c) Calculate the volume of the solid by integrating  $A(x)$  over an appropriate interval.
  
3. Find the volume of the solid formed by rotating the area bounded by  $f(x) = (x - 2)^3$ , the  $x$ -axis, and  $x = 3$  about  $x = 1$ .
  
4. Find the volume of the solid formed by rotating the area bounded by  $y = \frac{1}{2}x - 1$  and the  $x$  and  $y$  axes about  $y = -3$ .